# NEW YORK CITY COLLEGE OF TECHNOLOGY The City University of New York 

## DEPARTMENT:

## COURSE:

TITLE:

DESCRIPTION:

TEXT:

CREDITS:

PREREQUISITE:

MAT 2680
Differential Equations
An introduction to solving ordinary differential equations. Applications to various problems are discussed.

William T. French, Elementary Differential Equations Free Edition 1.01, December 2013

3 (3 class hours)
MAT 1575

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Fall 2018
Updated Spring 2021
A. Testing Guidelines:

The following exams should be scheduled:

1. Three one-session exams
2. A one session Final Examination.

| Course Learning Outcomes | General Education <br> Learning Outcomes | Flexible Core- <br> Scientific World |
| :--- | :--- | :--- |
| Be able to identify the type of <br> differential equation and choose <br> the appropriate methods to <br> solve the problem | Be able to use the existing <br> knowledge to choose a proper <br> method to accomplish the <br> problem. | Evaluate evidence and <br> arguments critically or <br> analytically |
| Be able to solve first order <br> linear and nonlinear equations <br> by implementing knowledge <br> from Calculus | Be able to transfer the <br> knowledge of calculus to solve <br> differential equation problems | Produce well-reasoned written <br> arguments using evidence to <br> support conclusions |
| Be able to model real world <br> problems using first order <br> differential equations and <br> understand the model <br> prediction | Be able to see the connection to <br> experience | Gather, interpret, and assess <br> information from a variety of <br> sources and points of view. |
| Be able to solve second order <br> linear differential equations <br> with various methods | Be able to use the existing <br> knowledge to choose a proper <br> method to accomplish the <br> problem. Complete the <br> mathematical analysis and draw <br> proper conclusion. Understand <br> the limitation of each method. | Understand the scientific <br> principles underlying matters of <br> policy or public concern in <br> which science plays a role |
| Produce well-reasoned written <br> arguments using evidence to <br> support conclusions. |  |  |
| Be able to model mechanical or <br> electrical problems using <br> second order differential <br> equations and understand the <br> model prediction <br> other disciplines | Identify and apply fundamental <br> concepts and methods of <br> mathematics to explore the <br> engineering problems |  |
| Be able to solve differential <br> equations using power series <br> and be able to solve initial <br> value problems using Laplace <br> Transform | Be able to show integrated <br> communication through <br> completing the mathematical <br> reasoning of the problem | Be able to understand the <br> limitations and implications of <br> the method |
| Be able to use numerical <br> method to approximate solution <br> when appropriate | Be able to understand the <br> limitations and implications of <br> the method | Demonstrate how tools of <br> science and mathematics can be <br> used to analyze problems and <br> develop solutions |
| Produce well-reasoned written |  |  |
| arguments using evidence to |  |  |
| support conclusions. |  |  |\(\left|\begin{array}{l}Produce well-reasoned written <br>

supports conclusions\end{array}\right|\)

## Course Intended Learning Outcomes/Assessment Methods

| Learning Outcomes | Assessment Methods |
| :--- | :--- |
| 1. Classify differential equations. | Classroom activities and discussion, <br> homework, exams |
| 2. Solve first and second order ordinary <br> differential equations using various techniques. | Classroom activities and discussion, <br> homework, exams |
| 3. Use numerical methods to approximate <br> solutions, when appropriate. | Take-home exam or project |
| 4. Apply methods of solving differential <br> equations to answer questions about various <br> systems (such as mechanical or electrical) | Classroom activities and discussion, <br> homework, exams |

## General Education Learning Outcomes/Assessment Methods

| Learning Outcomes | Assessment Methods |
| :--- | :--- |
| 1. Gather, interpret, evaluate, and apply <br> information discerningly from a variety of <br> sources. | Classroom activities and discussion, <br> homework, exams |
| 2. Understand and employ both quantitative and <br> qualitative analysis to solve problems. | Classroom activities and discussion, <br> homework, exams |
| 3. Employ scientific reasoning and logical <br> thinking. | Classroom activities and discussion, <br> homework, exams |
| 4. Communicate effectively. | Classroom activities and discussion, <br> homework, exams |

## New York City College of Technology Policy on Academic Integrity

Students and all others who work with information, ideas, texts, images, music, inventions, and other intellectual property owe their audience and sources accuracy and honesty in using, crediting, and citing sources. As a community of intellectual and professional workers, the College recognizes its responsibility for providing instruction in information literacy and academic integrity, offering models of good practice, and responding vigilantly and appropriately to infractions of academic integrity. Accordingly, academic dishonesty is prohibited in The City University of New York and at New York City College of Technology and is punishable by penalties, including failing grades, suspension, and expulsion. The complete text of the College policy on Academic Integrity may be found in the catalog.

MAT 2680 Differential Equations
Text: W.F.Trench, Elementary Differential Equations, Free Edition 1.01

| Session | Section and Topic | Pages | Homework |
| :---: | :---: | :---: | :---: |
| 1 | 1.2 First Order Equations [OPTIONAL: 1.3 Direction Fields for First Order Equations] | $\begin{aligned} & 7-13 \\ & 16-17 \end{aligned}$ | p.14: 1, 2(a-c,e-h), 4(a-f), 5, 6, [optional: p. 14: 9 and p. 21: 1-11] |
| 2 | 2.1 Linear First Order Equations | 30-41 | p.41: 1-9 odd, 17-23 odd, 31-37 odd, 38, 40, 42 |
| 3 | 2.2 Separable Equations | 45-52 | $\begin{aligned} & \text { p.52: } 2,3,6,12,17-27 \text { odd, } 28 \text {, } \\ & 35,37 \end{aligned}$ |
| 4 | 2.4 Transformation of Nonlinear Equations into Separable Equations | 62-68 | $\begin{aligned} & \text { p.68: 1-4, 7-11 odd, 15-18, 23-27 } \\ & \text { odd } \end{aligned}$ |
| 5 | 2.5 Exact Equations | 73-79 | p.79: 1-21 odd, 29, 30, 33, 34 |
| 6-7 | 4.1 Growth and Decay <br> 4.2 Cooling and Mixing <br> 4.3 Elementary Mechanics | $\begin{aligned} & 130-137 \\ & 140-147 \\ & 151-160 \end{aligned}$ | $\begin{aligned} & \text { p. 138: } 1-7 \text { odd, } 11,13,17 \\ & \text { p. } 148: 1-11 \text { odd, } 15 \\ & \text { p. } 160: 3,5,7,10 \end{aligned}$ |
| 8 | First Examination |  |  |
| 9 | 3.1 Euler's Method | 96-106 | $\begin{aligned} & \text { p.106: 1-7 odd, 11-13, 15-19 odd, } \\ & 20-22 \end{aligned}$ |
| 10 | 3.2 The Improved Euler Method and Related Methods | 109-116 | $\begin{aligned} & \text { p.116: 1-7 odd, 11-13, 15-19 odd, } \\ & 20-22 \end{aligned}$ |
| 11 | 3.3 The Runge-Kutta Method | 119-124 | $\begin{aligned} & \text { p.124: 1-7 odd, 11-13, 15-19 odd, } \\ & 20-22 \end{aligned}$ |
| 12 | 5.1 Homogeneous Linear Equations | 194-203 | p.203: 1-5 |
| 13 | 5.2 Constant Coefficient Homogeneous Equations | 210-217 | p.217: 1-17 odd, 18-21 |
| 14 | 5.3 Nonhomogeneous Linear Equations | 221-227 | p.227: 1-5 odd, 9-13 odd, 16-20 even, 25-29 odd, 33-37 odd |
| 15 | 5.4 The Method of Undetermined Coefficients I | 229-235 | p.235: 1-29 odd |
| 16 | 5.6 Reduction of Order | 248-252 | p.253: 1-3, 5, 9, 13, 17, 19, 25, 31 |


| 17 | 5.7 Variation of Parameters | 255-262 | p.262: 1-5, 7, 11, 13, 31, 33, 34 |
| :---: | :---: | :---: | :---: |
| 18 | Second Examination |  |  |
| 19 | 6.1 Spring Problems I 6.2 Spring Problems II | $\begin{aligned} & 268-277 \\ & 279-284 \end{aligned}$ | $\begin{aligned} & \text { p.277: 1, 3, 7-13 odd, 19, } 21 \\ & \text { p.288: 3, 4, 7-11 odd, 14-16 } \end{aligned}$ |
| 20 | 6.2 Spring Problems II (continued) <br> 6.3 The RLC Circuit | $\begin{aligned} & 284-287 \\ & 290-295 \end{aligned}$ | $\begin{aligned} & \text { p.288: } 13,17-20 \\ & \text { p.295: } 1-10 \end{aligned}$ |
| 21 | 7.1 Review of Power Series <br> 7.2 Series Solutions Near an Ordinary Point I | $\begin{aligned} & 307-316 \\ & 320-328 \end{aligned}$ | $\begin{aligned} & \text { p.317: 1, 11, 13, 15-17 } \\ & \text { p.329: } 1,3,8,11-13,19-25 \text { odd } \end{aligned}$ |
| 22 | 7.3 Series Solutions Near an Ordinary Point II | 335-338 | p.338: 1-5 odd, 19-23 odd, 33-37 odd, 41-45 odd |
| 23 | 7.4 Regular Singular Points Euler Equations | 344-346 | p.347: 1-12 |
| 24 | Third Examination |  |  |
| 25 | 8.1 Introduction to the Laplace Transform | 394-402 | $\begin{aligned} & \text { p. } 403: 1(\mathrm{a}, \mathrm{~b}, \mathrm{~d}, \mathrm{e}), 2(\mathrm{~b}, \mathrm{c}, \mathrm{f}, \mathrm{~g}, \mathrm{~h}, \mathrm{i}), 4 \text {, } \\ & 5,18 \end{aligned}$ |
| 26 | 8.2 The Inverse Laplace Transform <br> [NOTE: use the table on p. 463 of the textbook to do the homework] | 405-412 | $\begin{aligned} & \text { p.412: 1(a,b,d,e), 2(a-e), 3(a-d), } \\ & 4(a, d, e), 6(a), 7(a), 8(a, d) \end{aligned}$ |
| 27 | 8.3 Solution of Initial Value Problems <br> [NOTE: use the table on p. 463 of the textbook to do the homework] | 414-419 | p.419: 1-31 odd |
| 28 | 8.6 Convolutions <br> [NOTE: use the table on p. 463 of the textbook to do the homework] | 441-445 | p.450: 2(a,b,c,i,j,l,n), 3(a-c,e-g) |
| 29 | Review |  |  |
| 30 | Final Examination |  |  |


| MAT 2680 Differential Equations |  |
| :--- | :--- |
| Section and Topic |  |
| 1.2 First Order Equations | Homework |
| 1.3 Direction Fields for First Order Equations (optional) |  |
| 2.1 Linear First Order Equations |  |
| 2.2 Separable Equations |  |
| 2.4 Transformation of Nonlinear Equations into Separable Equations |  |
| 2.5 Exact Equations |  |
| 3.1 Euler's Method |  |
| 3.2 The Improved Euler Method and Related Methods |  |
| 3.3 The Runge-Kutta Method |  |
| 4.1 Growth and Decay |  |
| 4.2 Cooling and Mixing |  |
| 4.3 Elementary Mechanics |  |
| 5.1 Homogeneous Linear Equations |  |
| 5.2 Constant Coefficient Homogeneous Equations |  |
| 5.3 Nonhomogeneous Linear Equations |  |
| 5.4 The Method of Undetermined Coefficients I |  |
| 5.6 Reduction of Order |  |
| 5.7 Variation of Parameters |  |
| 6.1 Spring Problems I |  |
| 6.2 Spring Problems II |  |
| 6.2 Spring Problems II (continued) |  |
| 6.3 The RLC Circuit |  |
| 7.1 Review of Power Series |  |
| 7.2 Series Solutions Near an Ordinary Point I |  |
| 7.3 Series Solutions Near an Ordinary Point II |  |


| 7.4 Regular Singular Points Euler Equations |  |
| :--- | :--- |
| 8.1 Introduction to the Laplace Transform |  |
| 8.2 The Inverse Laplace Transform |  |
| [NOTE: use the table on p.463 of the textbook to do the homework] |  |
| 8.3 Solution of Initial Value Problems |  |
| [NOTE: use the table on p.463 of the textbook to do the homework] |  |
| 8.6 Convolutions |  |
| [NOTE: use the table on p.463 of the textbook to do the homework] |  |

